What happened on Laylatul Qadr?
The Qur'an was revealed to Muhammad (salla Allahu alayhi wa sallam) during Ramadan on Laylatul Qadr.

What happens on Laylatul Qadr?
The angels and the Ruh—Angel Jibreel (alayhi sallam) descend (come down) with the decrees (orders or decisions) of Allah (for the coming year).
When is Laylatul Qadr?

Look for it
in the last 10 nights of Ramadan

Bukhari : Book 8 : Volume 73 : Hadith 75

Narrated 'Ubada bin As-Samit:
Allah’s Apostle went out to inform the people about the (date of the Night of decree (Al-Qadr). There happened a quarrel between two Muslim men. The Prophet said, “I came out to inform you about the Night of Al-Qadr, but as so-and-so and so-and-so quarrelled, so the news about it had been taken away; and may be it was better for you. So look for it in the ninth, the seventh, or the fifth (of the last ten days of Ramadan).”

What are some signs of Laylatul Qadr?

"Verily, the sign of the Night of Al-Qadr is that it is pure and glowing as if there was a bright, tranquil, calm moon during it. It is not cold, nor is it hot, and no shooting star is permitted until morning. Its sign is that the sun appears on the morning following it smooth having no rays on it, just like the moon on a full moon night. Shaytan is not allowed to come out with it (the sun) on that day”.

Tafsir Ibn Kathir
What Surah Tells Us About Laylatul Qadr?

Suratul Qadr (97)
In the Name of Allah, the Most Gracious, the Most Merciful

1. Verily, We have sent it (this Quraan) down in the Night of Al-Qadr (Decree).

2. And what will make you know what the Night of Al-Qadr (Decree) is?

3. The Night of Al-Qadr (Decree) is better than a thousand months (i.e. worshipping Allah in that night is better than worshipping Him a thousand months, i.e. 83 years and 4 months).

4. Therein descend the angels and the Ruh Jibreeîl (Gabriel) by Allah’s Permission with all Decrees.

5. (All that night), there is peace (and goodness from Allah to His believing slaves) until the appearance of dawn.
What should we do on Laylatul Qadr?

"Whoever stands (in prayer) during the Night of Al-Qadr with faith and expecting reward (from Allah), he will be forgiven for his previous sins."

[Fath Al-Bari 4294, and Muslim 1253]

Is Laylatul Qadr always on the same night each year?

The Night of Al-Qadr moves around (i.e., from year to year) throughout the last ten nights.

Tafsir Ibn Kathir
A Duaa for Laylatul Qadr

It is recommended that one say the following supplication a lot:

"O Allah! Verily, you are the Oft-Pardoning, You love to pardon, so pardon me."

This is due to what Imam Ahmad recorded from Aishah that she said "O Messenger of Allah! If I find the Night of Al-Qadr what should I say?" He replied,

Say: "O Allah! Verily You are the Oft-Pardoning, You love to pardon, so pardon me."

[Ahmad 6:182] via Tafsir Ibn Kathir

"Allahumma Innaka 'Afuwun Tuhibbul-'Afwa Fa' affoo 'annee."